非平衡プラズマの温度に関する統計力学的検討

Statistical-Mechanical Discussion on Temperatures of Non-Equilibrium Plasma

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It is well known that the electron energy distribution function (EEDF) F becomes far from a Maxwellian one in a weakly-ionized plasma [1]. However, chemical kinetics of counterparts of electron collisions are not often included in such calculations. We discussed the dissociation degree of oxygen molecule, with simultaneous solution of the two-term approximated Boltzmann equation [2]. Here, the definition of the "temperature" should be reconsidered from the statistical thermodynamic viewpoint, which has seldom been discussed. Let the internal energy U and the entropy S for electron gas in a weaklyionized plasma. Then, the first law of thermodynamics leads:

$$\left(\frac{\partial S}{\partial U}\right)_{V,N_i} = \frac{1}{T}.$$
 (1)

Here, we neglect change in its volume or electric potential. Hereafter, T in Eq. (1) is referred to as the thermodynamic electron temperature $T_{\rm e}^{\rm th}$. Meanwhile,

$$U = \langle \epsilon \rangle = \int_0^\infty \epsilon F(\epsilon) \mathrm{d}\epsilon.$$
 (2)

We can also calculate the Gibbs electron entropy as

$$S = -k \int_0^\infty F(\epsilon) \ln \left[F(\epsilon) \right] d\epsilon.$$
(3)

In the present study, we chose microwave discharge oxygen plasma in a cylindrical tube of 2.6 cm^{ϕ} with its discharge pressure 1 Torr. We fixed the electron density $N_{\rm e} = 2 \times 10^{11} {\rm cm}^{-3}$ and the gas temperature 1000 K.

Meanwhile, many researchers define the electron kinetic temperature T_{e}^{k} from U of Eq. (2) as follows [3]:

$$T_{\rm e}^{\rm k} = \frac{2}{3k}U,\tag{4}$$

since the kinetic temperature agrees with the equilibrium electron temperature for the plasmas with the Maxwellian EEDF. Although Alvarez *et al.* concluded that $T_{\rm e}^{\rm th} = T_{\rm e}^{\rm k}$ [3], they never solved chemical kinetics of discharge gases

of the plasmas. We found the bulk ($\epsilon \leq 8.4 \text{ eV}$) and tail regions ($\epsilon > 8.4 \text{ eV}$), which has different slopes with their temperatures T_1 and T_2 ($< T_1$), respectively. This is due to the electron-impact oxygen dissociation, which causes non-equilibrium for the EEPF.

Fig. shows a comparison between various temperatures defined to the oxygen plasma. It should be remarked that $T_{\rm e}^{\rm th} \neq T_{\rm e}^{\rm k}$, which does not agree with Alvarez *et al.*'s result [3]. It should be noted that the thermodynamic temperature $T_{\rm e}^{\rm th}$ is more close to T_1 , the electron temperature of the bulk component than $T_{\rm e}^{\rm k}$ is. Further thermodynamic discussion is necessary to understand the physical meaning of each temperature, particularly for the relevance to Tsallis entropy.

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Sources Sci. Technol. **14** 722 (2005).

[2] J. Konno, A. Nezu, H. Matsuura and H. Akatsuka: Tech. Meeting on Plasma Sci. Technol., IEE Japan, PST-13-63 (2013) [in Japanese].

[3] R. Alvarez, J. Cotrino and A. Palmero: EPL. **105** 15001 (2014).