A Verification Scenario of Nuclear Plus Interference Scattering Effects Using Neutron Incident Angle Distribution to the Wall in Beam-Injected Deuterium Plasmas^{*)}

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A verification scenario of knock-on tail formation in the deuteron distribution function due to nuclear plus interference scattering is presented by observing the incident angle distribution of neutrons in a vacuum vessel. Assuming a knock-on tail created in a ³He-beam-injected deuterium plasma, the incident angle distribution and energy spectra of the neutrons produced by fusion reactions between 1-MeV and thermal deuterons are evaluated. The relation between the neutron incident angle to the vacuum vessel and neutron energy is examined in the case of anisotropic neutron emission due to knock-on tail formation in neutral-beam-injected plasmas.

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1. Introduction

Energetic ions contribute to form knock-on tails in ion velocity distribution functions [1-3] due to nuclear plus interference (NI) scattering¹ [4, 5]. As a consequence of knock-on tail formation, the neutron emission spectrum is modified from a Gaussian distribution [1, 6-8]. It is well known that the fraction of transferred power from the energetic to bulk ions is increased by NI scattering [9, 10]. In such a case, the required power fraction to maintain the hot ion mode was obtained in a D-³He spherical tokamak reactor [11]. By detecting the non-Gaussian component in the neutron emission spectrum, the knock-on tail and NI scattering effects can be diagnosed. Previously, possible verification scenarios for knock-on tail formation have been studied using the neutron emission spectrum [7, 8]. However, the non-Gaussian component is several orders of magnitude less than the peak of the Gaussian distribution function; hence, it is susceptible to the effects of background noise.

In deuterium plasmas, energetic protons are produced by the D(d,p)T and ${}^{3}He(d,p){}^{4}He$ reactions. These protons, especially by the latter reaction, cause large NI scattering and contribute to the knock-on tail formation in the deuteron velocity distribution function [9–12] (modification of the neutron emission spectrum [8]). If a small amount of ³He is externally admixed, the knockon grows large because the proton production rate by the ³He(d,p)⁴He reaction is enhanced. The degree of enhancement of the D(d,p)T, T(d,n)⁴He, and ³He(d,p)⁴He fusion reaction rate coefficient in a ³He-beam-injected deuterium plasma has been evaluated [13].

In neutral-beam-injected (NBI) plasmas, the knockon tail in the ion velocity distribution function and the non-Gaussian component in the neutron emission spectrum have anisotropic distributions because beam particles are injected in a particular direction. An effect of the anisotropy of emitted neutrons appears when they collide with the first wall. In toroidal devices, even for an isotropic emission of the neutrons, it is well known that the neutron flux and wall loading depend on wall positions [14, 15]. Because incident neutrons produced by suprathermal reactions have an anisotropic spectrum, the incident directions of neutrons to the first wall are also anisotropic when the knock-on tail is formed. By grasping the combination of the incident angle and the wall position where the largest number of non-Gaussian neutrons is observed, we can determine the most suitable detector position and angle for the knock-on tail diagnosis. This trend could be seen in all

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¹ NI scattering is defined by subtracting Coulomb contributions from experimental data. It is also referred to as "nuclear elastic scattering (NES)".

we can obtain more detailed information to validate the knock-on tail formation due to NI scattering and its effects by looking at the neutron incident angle distribution to the first wall.

In this paper, we assumed a knock-on tail created in a ³He-beam-injected deuterium plasma confined in the Large Helical Device (LHD). The neutron incident angle distribution and energy spectrum produced by the reactions between 1-MeV and thermal deuterons to the first wall are evaluated using a kinetic model combined with orbit calculations. A correlation between the neutron energy and incident angle, and a scenario to verify the NI scattering effects using the neutron incident angle distribution are presented.

2. Analysis Model

We assumed that the ³He beam is tangentially injected at the magnetic axis $R_{ax} = 3.6$ m, and that the knock-on tail in the deuteron velocity distribution function is formed in the beam-injected direction. The deuteron velocity distribution is adopted from Ref. [8]. The density of 1-MeV deuterons is about 2×10^{11} m⁻³ keV⁻¹ when a 100-keV-³He beam is injected in the deuterium plasma. The bulkdeuteron density $n_d = 8 \times 10^{19}$ m⁻³, and the electron temperature $T_e = 20$ keV were assumed. The adopted deuteron distribution function is shown in Fig. 1.

The positions and directions of energetic deuteron at the instant when the $D(d,n)^3$ He reaction occurs are calculated by the orbit calculation with the LHD field B_{ax} = 2.74 T. The cross section for the $D(d,n)^3$ He reaction is taken from the work of Bosch *et al.* [16]. The orbit of a 1-MeV deuteron for 200 toroidal turns after it is generated at the magnetic axis with pitch angle 0° is used for this calculation as a test particle. The orbit for 10 toroidal turns in (a) the meridional plane and (b) the equatorial plane is shown in Fig. 2.

Neutron emission direction and energy are calculated using the positions, directions, and energies of the energetic deuterons. The neutron emission energy by the $D(d,n)^{3}$ He reaction in the laboratory system is written as follows [17]:

$$E_{\rm n} = \frac{1}{2} m_{\rm n} v_0^2 + \frac{m_{^3\rm He}}{m_{^3\rm He} + m_{\rm n}} (Q + E_{\rm r}) + v_0 \cos \zeta \sqrt{\frac{2m_{^3\rm He}m_{\rm n}}{m_{^3\rm He} + m_{\rm n}} (Q + E_{\rm r})},$$
(1)

where $m_{n(^{3}He)}$ is the neutron (³He) mass, v_{0} is the centerof-mass velocity of the reacting deuterons, ζ is the angle between the center-of-mass velocity and neutron velocity vectors in the center-of-mass system, Q is the reaction Q-value, and E_{r} is the relative energy of the reacting deuterons.

Neutron collision points with the first wall and neutron incident angles are calculated using the neutron emission direction and a mathematical expression of the shape



Fig. 1 Adopted deuteron distribution function [8]. The bulkdeuteron density $n_{\rm d} = 8 \times 10^{19} \,\mathrm{m^{-3}}$ and the electron temperature $T_{\rm e} = 20 \,\mathrm{keV}$ are assumed.



Fig. 2 Orbit of a 1-MeV deuteron for 10 toroidal turns in (a) the meridional plane, (b) the equatorial plane.

of the first wall. In this calculation, the shape of the vacuum vessel of the LHD as the first wall is assumed as a torus. The incident angle of the neutron to the first wall is calculated as the angle between the neutron emission direction and wall surface. We defined the incident angle ι_p , and in the meridional plane as the poloidal incident angle ι_p , and in the equatorial plane as the toroidal incident angle ι_t . The assumed first wall shape and defined incident angles in (a) the meridional plane and (b) the equatorial plane are shown in Fig. 3.

We assumed that neutrons by reactions of thermal deuterons are isotropically emitted from the inside of a torus with a major radius of 3.6 m and a minor radius of 0.3 m.



Fig. 3 Relations between the first wall shape and (a) the poloidal incident angle ι_p in the meridional plane and (b) the toroidal incident angle ι_t in the equatorial plane.



Fig. 4 Neutron emission spectrum by the $D(d,n)^3$ He reaction when the knock-on tail is formed in the deuteron distribution function.

3. Results and Discussion

3.1 Neutron emission spectrum

The neutron emission spectrum by the $D(d,n)^3$ He reaction is shown in Fig. 4. It is found that the non-Gaussian component is formed in the neutron emission spectrum with a range of energies from about 1.8 to 4.1 MeV, which is caused by the knock-on tail component in the deuteron velocity distribution function. The non-Gaussian component is about seven orders of magnitude smaller than the peak of the Gaussian component. However, because the non-Gaussian component has an anisotropic spectrum, the observed spectrum depends on the position and direction of the detector.

3.2 Neutron incident energy spectrum to the wall

The neutron incident energy spectra at (a) all wall positions and (b) $\theta = 0^{\circ}$ are shown in Fig. 5. It is found that the neutron incident spectrum depends on the wall position. At wall position $\theta = 0^{\circ}$, neutrons with a range of energies from about 1.8 to 4.1 MeV are observed. As can be seen from Eq. (1), the neutron emitted in the same direction as the center-of-mass velocity of the reacting deuterons has the maximum energy, and the neutrons emitted in the opposite direction has the minimum energy. As the ³He beam is injected tangentially in the equatorial plane and the



Fig. 5 Neutron incident energy spectra at (a) all wall positions, (b) $\theta = 0^{\circ}$.

knock-on tail is formed in the beam-injected direction, the neutrons that have maximum and minimum energies can be observed only at $\theta = 0^\circ$. In tangentially beam-injected plasmas, it can be said that the wall position $\theta = 0^\circ$ is the most suitable for neutron measurements aimed at verifying knock-on tail formation, because this position observes the neutrons with a full range of energies in the non-Gaussian component.

3.3 Neutron incident angle distribution to the wall

The toroidal incident angles and energy distributions of neutrons at $\theta = 0^{\circ}$ at (a) all toroidal incident angles and (b) $\iota_t = 45^{\circ}$ point are shown in Fig. 6. The neutron incident angle correlates closely with the neutron emission energy and direction. It is recognized that two peaks exist at about 1.8 and 4.1 MeV. The neutron incident angle is determined by the geometric relationship between the shape of the first wall and the neutron emission direction. Neutrons emitted in the same direction as the center-of-mass velocity of the reacting deuterons, collide with the first wall at an incident angle $\iota_t = 45^{\circ}$ and with maximum energy. In the same manner, neutrons with the minimum energy collide with the first wall at an incident angle $\iota_t = 135^{\circ}$.

At $\iota_t = 45^\circ$, the largest number of neutrons in the non-Gaussian component is observed and the non-Gaussian component is about five orders of magnitude smaller than



Fig. 6 Neutron incident energy spectra at the wall position $\theta = 0^{\circ}$ for (a) all toroidal incident angles, (b) $\iota_t = 45^{\circ}$.

2.5-MeV peak. The largest number of neutrons in the Gaussian component in the neutron emission spectrum is observed at the incident angles of 50° and 130°. When neutrons are isotropically emitted from a circumference with a radius of 3.6 m, they can collide with the first wall with incident angles within the interval of about $49^\circ \le \iota_t \le 131^\circ$. Therefore, it is difficult to observe neutrons by reactions of thermal deuterons at $\iota_t = 45^\circ$. If we observe the neutron spectrum at $\iota_t = 45^\circ$ point, the difference between the non-Gaussian and 2.5-MeV Gaussian peak is reduced by two orders of magnitude compared with the space-averaged neutron emission spectrum. This is advantageous for improving the precision of fast-ion diagnostics.

4. Conclusions

By assuming a knock-on tail is formed in a ³He-beaminjected deuterium plasma confined in the LHD, a scenario to validate the NI scattering effects using the incident angle distribution and energy spectrum of neutrons is presented. By examining the dependence of the neutron energy on the incident angle to the first wall for fusion reactions between 1-MeV and thermal deuterons, we found the most suitable position and angle for the neutron detector for diagnostics of knock-on tail formation. Furthermore, the difference between the non-Gaussian component and 2.5-MeV Gaussian peak in the neutron spectrum can be reduced by two orders of magnitude compared with the neutron emission spectrum.

In this paper, as a first step, it is shown that the differentiation of the neutron emission spectrum with respect to the incident angle is effective for knock-on tail diagnostics. The density, temperature, and spatial distribution of thermal deuteron are somewhat different from the LHD plasmas, because the calculation was made with reference to previous results [8]. To verify the NI scattering effects experimentally, the neutron incident angle and energy distribution should be evaluated considering the deuteron velocity distribution function with a full range of energies in the actual conditions of the LHD plasma. As the difference between the non-Gaussian component and 2.5-MeV Gaussian peak in the neutron emission spectrum is about four orders of magnitude [8], it is expected that the difference could be reduced to two orders of magnitude. A more detailed calculation with modifications to the analysis model (to consider the spatial and pitch-angle distributions of energetic deuteron and the actual shape of vacuum vessel of the LHD, etc.) is the subject of a future study.

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