Economic Analysis of Advanced Fuel Fusion Reactors and Derivation of Scaling Law for COE*)

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Social acceptance of fusion reactors depends largely on their economic viability. To investigate this issue, we estimate and compare the cost of electricity (COE) among D-T, D-³He, and D-D fusion reactors. Three types of confinement systems are evaluated: the tokamak reactor (TR), the spherical tokamak reactor (STR), and helical reactor (HR). For each reactor type, COE parameter surveys are performed and new scaling laws for COE are derived. The COE for D-³He and D-D is high and depends more strongly on plasma beta value and maximum magnetic field strength than that of D-T.

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1. Introduction

Research and development of fusion reactors has primarily focused on the D-T reaction. However, the 14 MeV neutrons produced by this reaction present engineering and safety problems. Therefore, an ultimate future target is to realize an advanced fuel fusion reactor based on the D-³He or D-D reaction.

Commercial fusion reactors must not only resolve the technical problems but be socially accepted as well. The latter is largely dependent on reactor fusion economics. In previous studies, we have investigated the economics of D-T, D-³He and D-D fuel fusion reactors in Tokamak and spherical Tokamak confinement systems [1]. In the present study, we newly evaluate the economics of helical reactors, and perform an extensive parameter survey that clarifies the factors predominantly affecting the economics of advanced fuel fusion reactors.

The economics of D-T fusion reactors has been found to follow a scaling law [2, 3]. In this paper, we derive new scaling laws for the economics of D-T, D-3He and D-D fusion reactors.

2. Analysis Procedures

The cost of electricity (COE) for fusion reactors is calculated from the physics–engineering–cost (PEC) system code (Fig. 1) [4]. The radial build of fusion-island (FI) components such as blanket and shield is mainly determined from the major radius of the plasma R_p and the component thickness. The volume and weight of each FI component is calculated from the radial build, and is mul-

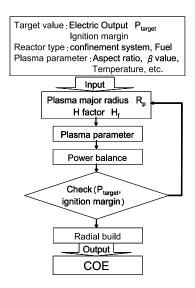


Fig. 1 Flowchart of the PEC code.

tiplied by its unit cost to obtain the cost of the component. The cost of balance of plant (BOP), such as the turbine and the main heat transport system, is estimated from scaling formulas of net electrical and thermal outputs.

3. Reactor Model

We considered three types of confinement system and three types of fuel cycles (a total of nine reactor types), whose input and calculated parameters are listed in Table 1. The following input parameters were fixed: target net electric power of 1000 MW, plant availability of 75%, operating period 30 years, and target ignition margin of 1.01. Here, the ignition margin is refined by the ratio of the heating power of charged particles (produced by the

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Table 1 Main input and calculated parameters for reference reactor types.

Confinement system		TR			STR			HR	
Fuel cycle	D-T	D-3He	D-D	D-T	D-3He	D-D	D-T	D- ³ He	D-D
Net electric power P_{enet} (GW)	1	1	1	1	1	1	1	1	1
Normalized beta β_N^a	4	8	8	8	8	8	(7)	(16)	(16)
Average beta value $\langle \beta \rangle$ (%)	5.27	10.55	10.55	30.19	30.19	30.19	5.00	12.00	12.00
Aspect ratio A ^a	3.54	3.54	3.54	1.62	1.62	1.62	7.81	7.81	7.81
Ellipticity κ^{a}	2.00	2.00	2.00	3.50	3.50	3.50	2.00	2.00	2.00
Maximum field B_{max} (T) ^a	13	13	13	8.75	13	13	13	13	13
Central ion temperature $T_i(0)$ (KeV) ^a	30	70	70	30	70	70	20	70	70
Maximum coil current density J_{max} (MA/m ²) ^a	30	30	30	13	30	30	30	30	30
Plasma major radius R_p (m)	6.33	11.52	10.90	3.98	8.23	7.94	14.31	16.03	17.62
Toroidal field B_t (T)	6.13	8.08	8.07	2.34	3.62	3.57	4.35	8.05	7.31
Fusion power (GW)	3.35	3.09	2.79	4.56	2.96	2.69	2.36	2.40	2.32
Neutron power (GW)	2.68	0.07	0.55	3.65	0.07	0.53	1.88	0.06	0.46
Ohmic loss (GW)				0.96					
Power density (MW/m ³)	4.61	0.71	0.75	3.18	0.23	0.24	1.24	0.90	0.65
Plasma current (MA)	14.49	34.72	32.81	21.64	69.40	66.00	0.00	0.00	0.00
Current drive power (MW)	138.82	87.86	78.32	10.55	72.01	64.21	0.00	0.00	0.00
HH factor $(H_{\rm ITER}, H_{\rm ISS})$	1.21	3.27	4.13	1.74	2.97	3.41	4.63	18.94	21.04
Density limit $\overline{n}/n_{\text{GW}}$	1.12	2.31	2.18	1.17	1.61	1.53	(2.05)	(2.93)	(2.94)
Density limit $\overline{n}/n_{\text{LHD}}$	(0.66)	(0.97)	(1.04)	(1.08)	(1.49)	(1.60)	0.88	0.80	0.89
COE (cent/kWh)	10.89	13.09	13.33	10.26	14.40	14.69	11.55	17.12	20.10
Neutron wall load (MW/m ²)	3.54	0.03	0.25	4.99	0.02	0.18	1.08	0.03	0.17

^a Input parameters

fusion reaction) to the loss power (including power lost by radiation).

3.1 Confinement systems

The confinement systems adopted here are the tokamak reactor (TR), spherical tokamak reactor (STR) and Helical Reactor (HR). The aspect ratio (A) and normalized beta value (β_N) of the TR reactor were set as 3.54 and 4 (D-T), respectively. D-³He and D-D ($\beta_N = 8$) are assigned a high β_N . In the STR, we can omit the inner blanket and use a normal conducting coil system for the center post coil, permitting a low aspect ratio (A = 1.62). Because a high beta value is expected in the ST, we again assume $\beta_N = 8$. However, the use of a normal conducting coil (maximum field strength $B_{\text{max}} = 8.75$) requires that some of the electricity output by the STR compensates for power lost by ohmic heating in the coil system. In the TR and STR, the current drive power $P_{\rm CD}$ depends on the average electron density $\langle n \rangle$, R_P , the plasma current I_P , and the bootstrap current I_{BS} ; more specifically, $P_{CD} = 2.0 \langle n \rangle R_P (I_P - I_{BS})$. Since the HR confinement system does not use plasma current, this system requires no external current drive power. The reference blanket model of TR and STR is Li₂O/FS, as in the Steady-State Tokamak reactor (SSTR) [5], while that of HR is Flibe/FS, as in the Force-Free Helical Reactor (FFHR) [6]. The electron and ion temperatures are assumed equal. Plasma density and temperature radial profiles are assumed parabolic: $n(r) = n_0(1 - r^2)^{0.25}$ and $T(r) = T_0(1 - r^2)^1$, where T_0 and n_0 are the central temperature and density, respectively, and r is the normalized small radius.

3.2 Fuel cycle

We evaluated three types of fuel cycles: D-T, D-3He and D-D. Since D-³He reactors generate very few neutrons and do not breed tritium, these reactors are not supplied with a breeding blanket. The shield thickness of a D-3He TR is assumed as 0.7 m, as in ARIES-3 [7]. Since ³He gas is a very rare terrestrial resource, we assumed a scenario in which ³He is transported from the lunar surface and estimated its cost as 200 US\$/g [8]. The D-D reactor system recycles T and ³He produced by the D-D reaction and extracts energy from D-T and D-3He reactions (catalyzed D-D). The respective inboard and outboard blanket thicknesses of D-D TR are 0.21 and 0.41 m, whereas the inboard and outboard shield thicknesses are 0.44 and 1.00 m, as seen in WILDcat [9]. In STR, because of low neutron wall load for the D-3He and catalyzed D-D reactors, we set the inboard shield thickness as 0.56 m for both D-3He [10] and D-D, and suppose that STR uses a superconducting coil ($B_{\text{max}} = 13 \text{ T}$). The ratio of ion to electron density (n_i/n_e) is assumed as 1.00 (D-T), 0.66, (D- 3 He), 0.90 (D-D).

4. Assessment Results

4.1 Parameter dependence

For each type of reactor, we calculated the dependence of COE on beta value (β) , maximum magnetic field (B_{max}) , net electric power (P_{enet}) , and thermal efficiency (f_{th}) , using the parameters from Table 1. The results for TR, STR, and HR are shown in Figs. 2, 3, and 4, respectively. Since higher β and B_{max} characterize higher plasma density, they are also associated with higher power density. Consequently, the plasma volume that satisfies P_{enet} is re-

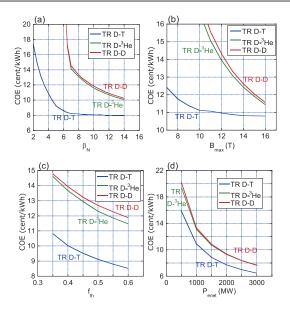


Fig. 2 Dependence of COE on (a) $\beta_{\rm N}$, (b) $B_{\rm max}$, (c) $f_{\rm th}$ and (d) $P_{\rm enet}$ of TR.

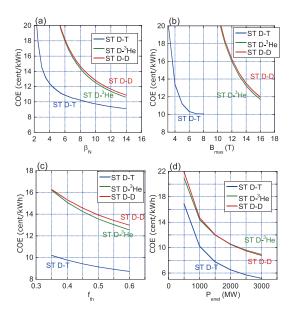


Fig. 3 Dependence of COE on (a) $\beta_{\rm N}$, (b) $B_{\rm max}$, (c) $f_{\rm th}$ and (d) $P_{\rm enet}$ of STR.

duced and a smaller reactor is required, reducing both the construction cost and COE. Since the reaction rate of an advanced fuel fusion reactor is very low, the COE for such a reactor is higher than that of D-T.

In TR, the bootstrap current ratio is assumed to be a function of poloidal beta value. At $\beta_{\rm N}$ < 7, the bootstrap current ratio is < 95%. Because a low bootstrap current ratio requires high current drive power, the power of the circulating electricity increases, along with the required fusion power. As a result, the COE in advanced fuel reactors is also increased by low bootstrap current ratio.

Since the STR D-T reactor uses a normal conducting coil system, we assume a small value of B_{max} in this reac-

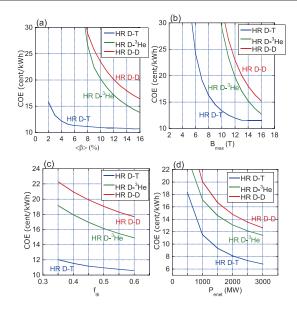


Fig. 4 Dependence of COE on (a) $\langle \beta \rangle$, (b) B_{max} , (c) f_{th} and (d) P_{enet} of HR.

Table 2 Design parameters for scaling laws.

		$\beta_{\rm N}, \langle \beta \rangle$ (%)	$B_{\text{max}}(T)$
TR	D-T	2-5	10–16
	D-T D- ³ He,D-D	6–14	10-16
STR	D-T	6-12	4-10
	D-T D- ³ He,D-D	6-14	10-16
HR	D-T	2–6	10-16
	D- ³ He,D-D	6–14	10–16

tor. Moreover, the power of the circulating electricity must be increased to compensate for ohmic heating loss in the coil.

In the advanced fuel reactor of HR, the COE strongly depends on beta value and magnetic field strength, and the ISS confinement scaling law specifies an extremely high H factor. Thus, the confinement requires much improvement in the high temperature regime of HR.

In all reactors types, the COE is reduced by high $f_{\rm th}$ and $P_{\rm enet}$. In particular, high-powered reactors incur small COE.

4.2 COE scaling laws

In addition to the survey parameters, the design parameters were the plant availability ($f_{\rm avail}$) and operating period ($t_{\rm oper}$). The COE scaling laws were derived from multiple regression analysis. The ranges of β and $B_{\rm max}$ are listed in Table 2; $P_{\rm enet}$ covers 0.5 - 3.0 GW, $f_{\rm avail}$ is 0.65 - 0.8, $t_{\rm oper}$ is 20 - 40 year and $f_{\rm th}$ is 0.35 - 0.60. The new scaling laws are derived as follows.

$$COE^{\text{TRD-T}}[\text{cent/kWh}] = 10^{2.36} \frac{1}{\beta_{\text{N}}^{0.54} B_{\text{max}}^{0.11} P_{\text{enet}}^{0.53} f_{\text{avail}}^{0.91} t_{\text{oper}}^{0.79} f_{\text{th}}^{0.48}},$$
 (1)

$$COE^{\text{TRD-}^{3}\text{He}}[\text{cent/kWh}] = 10^{3.49} \frac{1}{\beta_{\text{N}}^{0.83} B_{\text{max}}^{0.52} P_{\text{enrt}}^{0.56} f_{\text{avail}}^{0.92} f_{\text{oper}}^{0.82} f_{\text{th}}^{0.39}},$$
 (2)

$$COE^{\text{TRD-D}}[\text{cent/kWh}] = 10^{3.67} \frac{1}{\beta_{\text{N}}^{0.86} B_{\text{max}}^{0.60} P_{\text{enet}}^{0.58} f_{\text{avail}}^{0.95} f_{\text{oper}}^{0.85} f_{\text{th}}^{0.37}},$$
 (3)

$$COE^{\text{STD-T}}[\text{cent/kWh}] = 10^{2.53} \frac{1}{\beta_{\text{N}}^{0.33} B_{\text{max}}^{0.30} P_{\text{enet}}^{0.62} f_{\text{avail}}^{0.95} t_{\text{oper}}^{0.82} f_{\text{th}}^{0.33}},$$
(4)

$$COE^{\text{STD-}^{3}\text{He}}[\text{cent/kWh}] = 10^{4.05} \frac{1}{\beta_{\text{N}}^{0.67} B_{\text{max}}^{1.14} P_{\text{enet}}^{0.48} f_{\text{avail}}^{0.94} f_{\text{oper}}^{0.85} f_{\text{th}}^{0.48}},$$
 (5)

$$COE^{\text{STD-D}}[\text{cent/kWh}] = 10^{4.01} \frac{1}{\beta_{\text{N}}^{0.62} B_{\text{max}}^{1.09} P_{\text{enet}}^{0.55} f_{\text{avail}}^{0.96} f_{\text{oper}}^{0.87} f_{\text{th}}^{0.40}},$$
 (6)

$$COE^{\text{HRD-T}}[\text{cent/kWh}] = 10^{2.97} \frac{1}{\langle \beta \rangle^{0.33} B_{\text{max}}^{0.60} P_{\text{enet}}^{0.54} f_{\text{avail}}^{0.92} t_{\text{th}}^{0.84} f_{\text{th}}^{0.34}},$$
(7)

$$COE^{\text{HRD}-^{3}\text{He}}[\text{cent/kWh}]$$

$$= 10^{6.13} \frac{1}{\langle \beta \rangle^{1.35} B_{\text{max}}^{2.11} P_{\text{enet}}^{0.46} f_{\text{avail}}^{0.96} t_{\text{the}}^{0.91} f_{\text{th}}^{0.52}},$$
(8)

$$COE^{\text{HRD-D}}[\text{cent/kwh}] = 10^{5.85} \frac{1}{\langle \beta \rangle^{1.16} B_{\text{max}}^{1.98} P_{\text{enet}}^{0.46} f_{\text{avail}}^{0.92} t_{\text{th}}^{0.92} f_{\text{th}}^{0.50}}.$$
 (9)

In D-³He and D-D, the β and B_{max} exponents exceed those of D-T, and the COE of these advanced fusion reactors strongly depends on β and B_{max} .

5. Summary

We have calculated the COE of advanced fuel fusion

reactors in three types of confinement systems and derived new scaling laws for the COE of advanced fuel reactors.

Since the reaction rate in advanced fuel fusion reactors is very low, more plasma volume is required than in the D-T reactor to produce the same target net electric power. Therefore the plant construction cost, and consequently the COE, is increased. To achieve COE similar to that of the D-T Tokamak reactor TR ($\beta_N = 4$), the β_N should be raised in the D-³He and D-D TR reactors ($\beta_N > 10$). However, high β_N (> 5) is not readily attained in a conventional TR. If high β_N could be realized in spherical tokamak confinement systems, together with high magnetic field generated by the superconducting coil, the COE of D-³He would become comparable to that of D-T.

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