

# Field line tying and magnetic shear effects of the vertical magnetic field on low frequency density fluctuations in CPD

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The two dimensional structure of density fluctuations is examined in a microwave produced annulus plasma at  $B_t = 0.3$  T. In simple torus configuration low frequency coherent waves are found to be unstable and the density fluctuation level reaches to 30-40 %. By applying  $B_z$  field (50 G) it should be noted that the fluctuation level is reduced by 80 % and no coherent modes are found. The current ramp-up condition is discussed from a view point of the improved mode conversion of incident cyclotron waves with reduced fluctuations.

Keywords: non-inductive current drive, low frequency density fluctuations, EBW, ECW, Li sheet beam

## 1. Introduction

In the spherical tokamak device CPD (Compact Plasma wall interaction experimental Device), the non-inductive current drive experiments have been performed in hydrogen plasma using electron cyclotron waves [1]. At 1 kW of the rf power at 8.2 GHz an annulus plasma is initially produced near the resonance layer  $R_{res}$  (~0.16 - 0.19 m) and is extended radially up to ~ 0.1 m. With increasing the rf power the current  $I_p$  ramps up and via a current jump phenomenon closed magnetic surfaces are formed [1, 2]. Relatively higher vertical field  $B_z$  was found to be required to ramp up current even in the initial phase. This has been observed in CDX-U[3] and LATE[4]. Since both extraordinary (X) and ordinary (O) waves are launched from the low field side (LFS), they cannot access to the electron cyclotron resonance (ECR) beyond the cutoff layers (right-hand and plasma) without mode conversion to the electron Bernstein wave (B) [5, 6]. The conversion efficiency  $\eta_{XB}$  from X to B or transmission efficiency  $T_{OX}$  from O to X mode at the cutoff layer strongly depends on the density scale length  $L_n = n_e / |\partial n_e / \partial r|$ . In order to achieve high  $\eta_{XB}$  the short  $L_n$  of ~ 5 mm is required [7]. However, it has been

well known that the steep density gradient  $\nabla n_e$  drives density fluctuations in the toroidal device. Under such situations, since the conversion layer becomes rough and wavy due to fluctuations,  $T_{OX}$  is reduced at high  $\tilde{n}_e/n_e$  and high poloidal wave length  $\lambda_{pol}$  [8]. Using a simple spectrum of the poloidal refractive index  $T_{OX}$  is calculated as a function of  $L_n$  for various  $\tilde{n}_e/n_e$  as shown in Fig.1. Since  $\tilde{n}_e/n_e > 30-40$  % and wave length  $> 25$  mm are observed in the annulus plasma, these fluctuations must be stabilized from a view point of higher mode conversion efficiency which is required to heat plasma and drive plasma current. Although both drift and flute modes driven by a steep  $\nabla n_e$  with  $L_n = 20-60$  mm have been studied in a simple torus BETA using 2.45GHz microwave, the effects of these waves on the X-B conversion have not been studied [9]. In this report we present the details of characteristics of the density fluctuations in the annulus plasma, and study the stabilization (field line tying [10] and magnetic shear [11]) effects of vertical field  $B_z$  on them in the weak mirror configuration.

## 2. Experimental Arrangement

### 2.1. CPD device and diagnostics

CPD is a spherical tokamak device whose diameter as well as height is ~ 1.2 m. The diameter of the center stack is 0.255 m. Mirror configurations (decay index ~ 0.046,  $B_z$  ~ 40 G at  $R=0.2$  m) are used to ramp-up  $I_p$ , which is measured with the Rogowski coil installed inside the CPD chamber.

A thermal Li sheet beam is injected from the bottom of the chamber and the 2D image of LiI (670.8 nm) is used to analyze the density profile [2,12,13]. The line averaged density is measured along the vertical chord at  $R=0.3$  m by an interferometer at 140 GHz. The scattered microwave component at the cutoff layer is monitored around the torus.

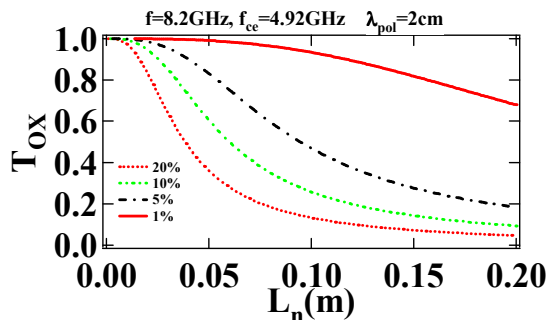


Fig.1  $T_{OX}$  v.s.  $L_n$  at  $f=8.2$  GHz.  $\tilde{n}_e/n_e=1\%$ (solid),  $5\%$ (dot-dashed),  $10\%$ (dashed), and  $20\%$ (dotted).  $\lambda_{pol}=2$  cm, and parallel refractive index  $N_{||}=0.7$ .

The X-wave reflected from the cutoff layer is measured with a reflectometer.  $T_e$  is measured by a scanning Langmür probe.

## 2.2. Li beam fluctuation spectroscopy (LBFS)

The LBFS system measures local, long wavelength ( $k_{\perp}\rho_s < 1$ ) density fluctuations by observing LiI. Fluctuations in LiI are proportional to the local density fluctuations,  $\tilde{n}_e/n_e = \tilde{I}_{Li}/I_{Li}$ . The radial resolution is  $\sim 5$  mm  $\phi$ . The LBFS system consists of 50 spatial points, connected to photomultiplier tubes via a fiber bundle. The image area is 50 mm  $\times$  25 mm. The sampling frequency of ADC is 300 kHz.

## 3. Measurement of Density Fluctuations

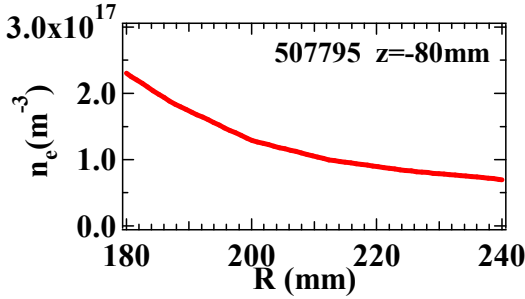


Fig.2 Density profile at  $z=-80$  mm.  $R_{res}=164$  mm.

### 3.1. Fluctuations in Annulus plasma

Characteristics of density fluctuations in initially produced annulus plasma are investigated. Since the plasma is vertically extended, the LiI intensity drops sharply for  $R < R_{res}$ , where flute modes are expected to be stable due to  $\vec{v}_n \cdot \vec{v}_B < 0$ , but it decays gradually for  $R > R_{res}$ , where flute modes become unstable due to  $\vec{v}_n \cdot \vec{v}_B > 0$ . The

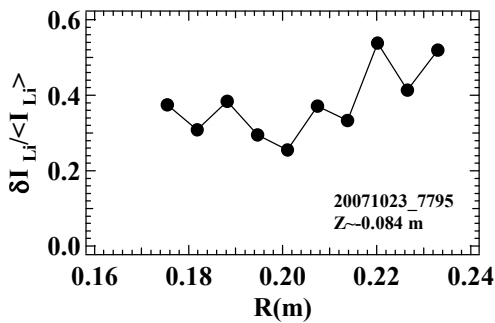


Fig.3  $\tilde{n}_e/n_e$  vs. R. Relative amplitude gradually increases along the major radius.

contour of the density aligns along the vertical direction [2] and the radial profile at  $Z = -80$  mm, as shown in Fig.2. According to the density profile with  $L_n \sim 40$  mm,  $R_{cutoff}$  and  $R_{UHR}$  are calculated to be 0.23 m and 0.19 m, respectively. Since this cutoff layer extends vertically, X-mode from LFS cannot access the resonance layer. Both flute and drift modes are also unstable in this region. Figure 3 shows a radial distribution of the relative

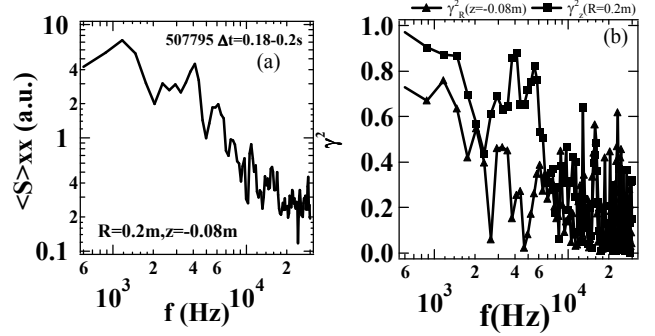


Fig.4 The auto power (a), and  $\gamma_R^2$  and  $\gamma_Z^2$  spectra (b).

fluctuation amplitude. The amplitude is 25-50 % around the expected mode conversion layer, which becomes rough and wavy due to fluctuations. The auto power spectrum  $S_{xx}$  and square coherency  $\gamma_R^2$  ( $\gamma_Z^2$ ) at two points separated by horizontal distance of  $\Delta R \sim 2.5$  cm (vertical distance of  $\Delta Z \sim 1.25$  cm) are analyzed by fast Fourier transform FFT, as shown in Fig.4. The time window is  $\sim 20$  ms and moving average at every 3.4 ms (1024 data

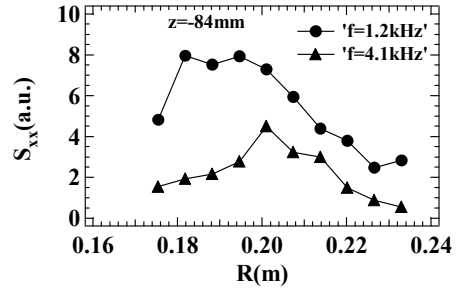


Fig.5 Radial profiles of  $S_{xx}$  at  $f=1.1$  and 4.1 kHz.

points) is used. The frequency resolution is 0.3 kHz.  $S_{xx}$  shows a broadband spectrum peaking at  $f \sim 1.1$  kHz and decaying to  $\sim 10$  kHz as  $f^{-1}$ . At  $f \sim 1.1$  kHz both  $\gamma_R^2$  and  $\gamma_Z^2$  are  $\geq 0.7$ , but, at  $f = 4.1$  kHz  $\gamma_R^2$  is reduced  $< 0.3$  while  $\gamma_Z^2 > 0.8$ . The radial profiles of  $S_{xx}$  at  $f=1.1$  and 4.1 kHz are shown in Fig. 5. The former shows a broad peak at 0.19 m and sharply decreases in the LFS. The latter also peaks at  $R \sim 0.2$  m and decays at both sides. Figure 6 shows that a mode at  $f=1.1$  kHz is extended coherent mode and a mode at 4.1 kHz is a relatively localized one. The radial correlation length for the 1.1 kHz mode is

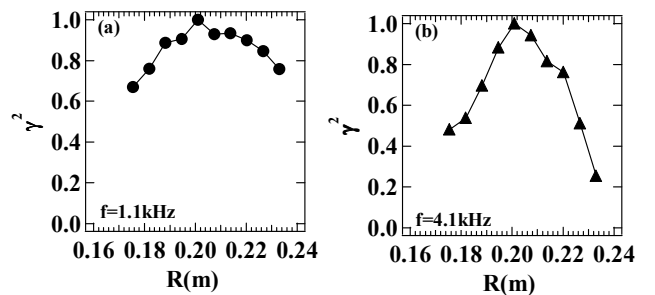


Fig.6 Radial profiles of  $\gamma_R^2$  at 1.1 (a) and 4.1 kHz (b).

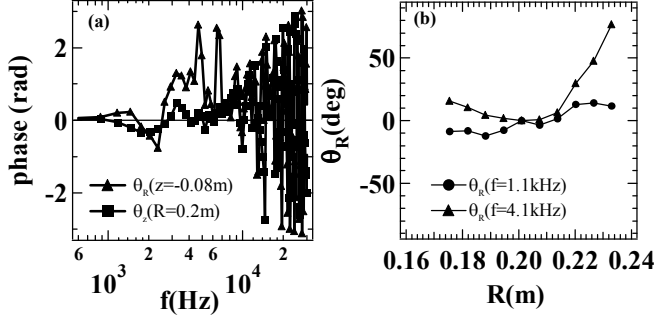


Fig.7 The cross phase  $\theta_R$  and  $\theta_Z$  spectra (a), radial profiles of  $\theta_R$  at  $f=1.1$  and  $4.1$  kHz.

considered to be longer than the viewing radial length of  $0.06$  m, and that for  $4.1$  kHz mode is  $< 0.03$  m. However, the vertical profiles of  $\gamma_Z^2$  shows a high coherence  $> 0.9$ , suggesting that both coherent modes are extended along the vertical direction. These modes are, therefore, expected to be aligned along the contour of the density. The cross phases  $\theta_R$  and  $\theta_Z$  at two points separated by  $\Delta R \sim 2.5$  cm ( $\Delta Z \sim 1.25$  cm) are also shown in Fig.7. The  $\theta_R$  spectrum rapidly deviates in the lower frequency range because the mode at  $4.1$  kHz is localized at  $R \sim 0.2$  m  $\pm 0.02$  m, on the other hand  $\theta_Z$  is remained around zero. These correspond to  $\gamma_R^2$  and  $\gamma_Z^2$  spectra in Fig. 4 (b). The mode at  $1.1$  kHz propagates along the major radius with a phase velocity of  $\sim 1$  km/s, as shown in Fig. 7(b). Since the variation in  $\theta_Z$  is within  $\pm 5$  deg at both frequencies, the wave number  $k_z$  along the vertical direction is  $\sim 0.01$   $\text{cm}^{-1}$ .

### 3.2. Stabilization in weak mirror configuration

As mention in §1, the necessary condition for current ramp-up is pre-applied vertical field, which is relatively higher from a view point of equilibrium. The reason why this condition is required has been partially studied as the uni-directional Pfirsch-Schlüter current along the inclined

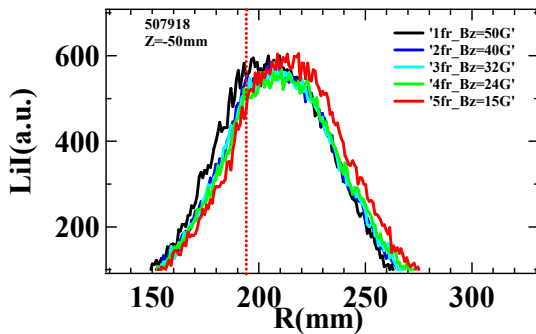


Fig.8 Radial profiles of  $\text{LiI}$  at  $z=-50$  mm below the equator at  $B_z = 15-50$  G. The dotted line corresponds to the resonance layer.

magnetic field or toroidal precession current due to the deeply trapped particles created by ECW[3,4]. However, the effects of density fluctuations have been never

considered. In this section how the  $B_z$  affects the density fluctuations will be presented.

In Fig. 8 the radial profiles of  $\text{LiI}$  images at various  $B_z$  values, indicating that  $B_z (< 50$  G) does not affect intensity profiles, namely the 2D structures of density. Since the effect of  $B_z$  on  $n_e(R, z)$  is insignificant, the driven force ( $\nabla n$ ) for the density fluctuations is also unchanged. However, it should be noted that the relative fluctuation amplitude decreases with increasing  $B_z$ , as shown in Fig. 9.

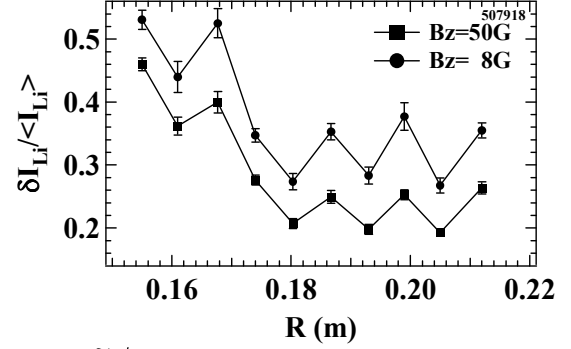


Fig. 9  $\tilde{n}_e/n_e$  vs.  $R$ . Two profiles taken at  $B_z=8$  and  $50$  G are shown.

In this experiment  $B_z$  was swept in step like manner for each 30 ms. Since resonance position is  $R_{\text{res}}=0.19$  m, the larger  $\tilde{n}_e/n_e$  might be driven by the steeper density gradient for  $R < R_{\text{res}}$ .

Although the reduction of relative amplitude is  $\sim 0.8$  by with  $B_z=50$  G at  $B_t=0.3T$ , the characteristics of the fluctuations are drastically changed. Auto power and square coherency spectra are shown in Fig.10. The integrated power in the low frequency range changes by a similar factor compared with that in the relative amplitude. The coherency and its spatial structure are quite drastically

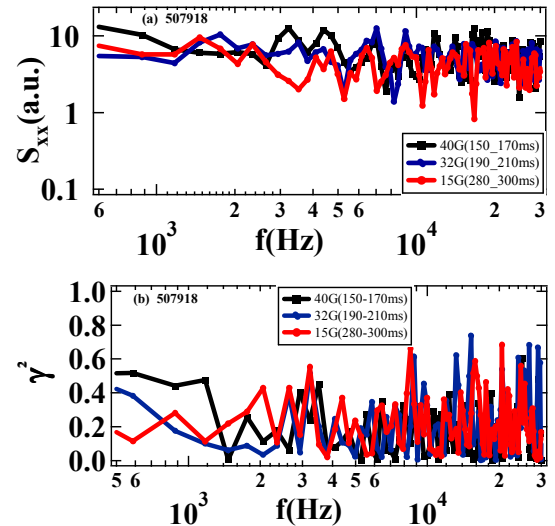


Fig. 10 The auto power (a), and square coherency  $\gamma^2$  spectra (b) at various  $B_z$ .

changed. Although coherent low frequency waves are unstable at  $B_z=0$  G, both coherencies between two horizontally and vertically separated points are much

reduced as  $B_z$  exceeds a certain value.

Figure 11 shows the stabilization effects of  $B_z$  on the

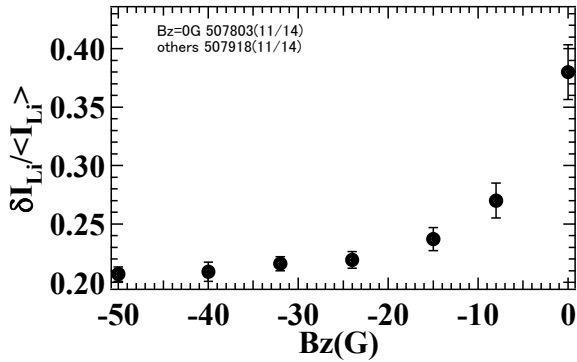


Fig. 11  $B_z$  dependence on  $\tilde{n}_e/n_e$  density fluctuation amplitude. Usually current ramp-up experiments have been done at relatively higher  $B_z$  value in a weak mirror configuration. According to result in Fig. 1 this stabilization effect is considered to be necessary for better conversion efficiency to EBW.

#### 4. Discussion

Changes in  $L_c$  and pitch angle are shown in Fig. 12. Here the connection length  $L_c$  is defined as the wall to wall length of the field lines, and pitch angle  $\theta = \tan^{-1}(B_z/B_r)$ . Since  $B_z$  is varied up to 50 G,  $L_c$  becomes shorter at higher  $B_z$ . For  $R < R_{\text{res}}$  the maximum of  $L_c$  is bounded by the case at  $B_z=15\text{G}$  and sharply decays towards the CS. On the other hand, it reduces gradually for  $R > R_{\text{res}}$ . In the region of interest  $L_c$  varies from 200 m to 70 m as  $B_z$  increases. Thus, stabilization effects of field line tying can be possible. Since the decay index of  $B_z$  is small and the radial variation of  $B_z$  is small, the magnetic shear length  $L_s = \theta / (d\theta/dR)$ , is an order of 0.2 m on the mid plane

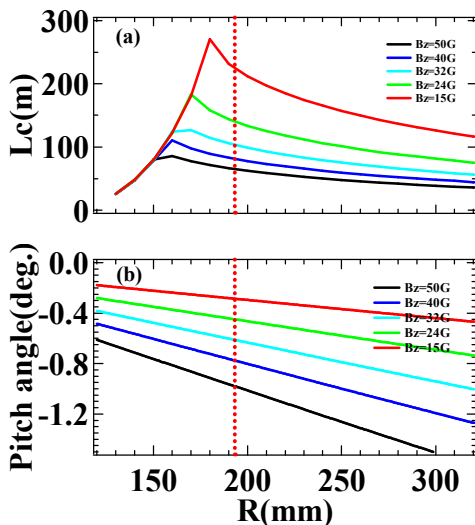


Fig.12 (a) The connection length  $L_c$  and (b) pitch angle  $\theta_{\text{pitch}}$  for various  $B_z$ . The dotted line indicates the resonance layer.

at  $R=R_{\text{res}}$  and it increases monotonically along  $R$ . Since  $L_s/L_n$  is an order of 5-10, the magnetic shear effects are also expected, as shown in Fig. 13.

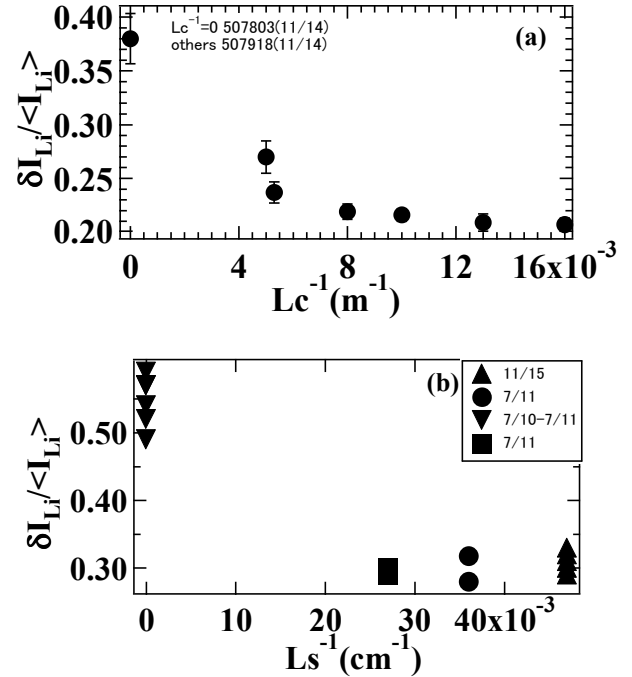


Fig. 13 The relative amplitude vs.  $L_c$  (a) and  $L_s$  (b)

#### 5. Conclusion

The 2 D structure of density fluctuations has been measured with LBFS in annulus rf plasma which has been produced by ECR. The equi-density contour is observed to be aligned along the vertical direction and coherent waves are found to be excited in the low frequency range (1-10 kHz). It should be noted that the vertical field, which is pre-required for ramp-up plasma current, stabilizes these coherent waves. The relative amplitude is reduced by a factor of 2 and the correlation length is reduced  $< 5\text{mm}$ . The line tying and magnetic shear effects seem to play more role in stabilization mechanisms.

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